ME - 2021

## APTITUDE

1. A digital watch $X$ beeps every 30 seconds while watch $Y$ beeps every 32 seconds. They beeped together at 10 A.M.

The immediate next time that they will beep together is $\qquad$
(a) 10.00 PM
(b) 11.00 AM
(c) 10.08 AM
(d) 10.42 AM
2. The front door of Mr. X's house faces East. Mr. X leaves the house, walking 50 m straight from the back door that is situated directly opposite to the front door. He then turns to his right, walks for another 50 m and stops. The direction of the point Mr . X is now located at with respect to the starting point is $\qquad$ -.
(a) West
(b) North-West
(c) South-East
(d) North-East
3. Given below are two statements 1 and 2 , and two conclusions I and II

Statement 1: All entrepreneurs are wealthy
Statement 2: All wealthy are risk seekers.
Conclusion I: All risk seekers are wealthy
Conclusion II: Only some entrepreneurs are risk seekers.
Based on the above statements and conclusions, which one of the following options is CORRECT?
(a) Only conclusion I is correct
(b) Neither conclusion I nor II is correct
(c) Both conclusions I and II are correct
(d) Only conclusion II is correct.

## TVTHE GATE COACH

4. The world is going through the worst pandemic in the past hundred years. The air travel industry is facing a crisis, as the resulting quarantine requirement for travellers led to weak demand.

In relation to the first sentence above, what does the second sentence do?
(a) Second sentence entirely contradicts the first sentence.
(b) The two statements are unrelated.
(c) Restates an idea from the first sentence
(d) States an effect of the first sentence.
5. The ratio of the area of the inscribed circle to the area of the circumscribed circle of an equilateral triangle is $\qquad$

(a) $\frac{1}{4}$
(b) $\frac{1}{6}$
(c) $\frac{1}{8}$
(d) $\frac{1}{2}$
6. Consider a square sheet of side 1 unit. The sheet is first folded along the main diagonal. This is followed by a fold along its line of symmetry. The resulting folded shape is again folded along its line of symmetry. The area of each face of the final folded shape, in square units, equal to $\qquad$ _.
(a) $\frac{1}{32}$
(b) $\frac{1}{8}$
(c) $\frac{1}{16}$
(d) $\frac{1}{4}$
7. Five persons $\mathrm{P}, \mathrm{Q}, \mathrm{R}, \mathrm{S}$ and T are to be seated in a row, all facing the same direction, but necessarily in the same order. P and T cannot be seated at either end of the row. P should not be seated adjacent to S . R is to be seated at the second position from the left end of the row. The number of distinct seating arrangement possible is:
(a) 3
(b) 5
(c) 4
(d) 2
8. A box contains 15 blue balls and 45 black balls. If 2 balls are selected randomly, without replacement, the probability of an outcome in which the first selected is a blue ball and the second selected is a black ball, is $\qquad$
(a) $\frac{3}{4}$
(b) $\frac{3}{16}$
(c) $\frac{45}{236}$
(d) $\frac{1}{4}$
9. Consider the following sentences:
(i) The number of candidates who appear for the GATE examination is staggering.
(ii) A number of candidates from my class are appearing for the GATE examination.
(iii) The number of candidates who appear for the GATE examination are staggering.
(iv) A number of candidates from my class is appearing for the GATE examination.

Which of the above sentences are grammatically CORRECT?
(a) (ii) and (iii)
(b) (i) and (iii)

## 【た THE GATE COACH

(c) (i) and (ii)
(d) (ii) and (iv)
10. If $\oplus \div \odot=2 ; \oplus \div \Delta=3 ; \odot+\Delta=5 ; \Delta \times \otimes=10$, then, the value of $(\otimes-\oplus)^{2}$, is :
(a) 1
(b) 4
(c) 16
(d) 0

## TVTHE GATE COACH

ME

1. A power transmission mechanism consists of a belt drive and a gear train as shown in the figure.


Diameters of pulleys of belt drive and number of teeth (T) on the gears 2 to 7 are indicated in the figure. The speed and direction of rotation of gear 7, respectively are:
(a) 575.28 rpm : clockwise
(b) 575.28 rpm : anticlockwise
(c) 255.68 rpm : anticlockwise
(d) 255.68 rpm : clockwise
2. A cast product of a particular material has dimensions $75 \mathrm{~mm} \times 125 \mathrm{~mm} \times 20 \mathrm{~mm}$. The total solidification time for the cast product is found to be 2.0 minutes as calculated using Chvorinov's rule having the index, $\mathrm{n}=2$. If under the identical casting conditions, the cast product shape is changed to a cylinder having diameter $=50 \mathrm{~mm}$ and height $=50 \mathrm{~mm}$, the total solidification time will be $\qquad$ minutes (upto 2 decimal places).
3. In a CNC machine tool, the function of an interpolator is to generate
(a) NC code from the part drawing during post processing.
(b) reference signal prescribing the shape of the part to be machined
(c) error signal for tool radius compensation during machining
(d) signal for the lubrication pump during machining.
4. Consider an ideal vapour compression refrigeration cycle working on $\mathrm{R}-134 \mathrm{a}$ refrigerant. The COP of the cycle is 10 and the refrigeration capacity is $150 \mathrm{~kJ} / \mathrm{kg}$. The heat rejected by the refrigerant in the condenser is $\qquad$ $\mathrm{kJ} / \mathrm{kg}$ (round off to the nearest integer).
5. Find the positive real root of $x^{3}-x-3=0$ using Newton-Raphson method. If the starting guess $\left(x_{0}\right)$ is 2 , the numerical value of the root after two iterations $\left(\mathrm{x}_{2}\right)$ is $\qquad$ (round off to the nearest integer).
6. The allowance provided in between a hole and a shaft is calculated from the difference between
(a) upper limit of the shaft and the lower limit of the hole
(b) lower limit of the shaft and the upper limit of the hole
(c) upper limit of the shaft and the upper limit of the hole
(d) lower limit of the shaft and the lower limit of the hole.
7. The Cast Iron which possesses all the carbon in the combined form as cementite is known as
(a) Grey Cast Iron
(b) Malleable Cast Iron
(c) Spheroidal Cast Iron
(d) White Cast Iron
8. An adiabatic vortex tube, shown in the figure given below is supplied with $5 \mathrm{~kg} / \mathrm{s}$ of air (inlet 1 ) at 500 kPa and 300 K . Two separate streams of air are leaving the device from outlets 2 and 3 . Hot air leaves the device at a rate of $3 \mathrm{~kg} / \mathrm{s}$ from the outlet 2 at 100 kPa and 340 K , while $2 \mathrm{~kg} / \mathrm{s}$ of cold air stream is leaving the device from outlet 3 at 100 kPa and 240 K .


Consider constant specific heat of air is $1005 \mathrm{~J} / \mathrm{kg} . \mathrm{K}$ and gas constant is $287 \mathrm{~J} / \mathrm{kg} . \mathrm{K}$. There is no work transfer across the boundary of this device. The rate of entropy generation is $\qquad$ $\mathrm{kW} / \mathrm{K}$ (round off to one decimal place).
9. The value of $\int_{0}^{\pi / 2} \int_{0}^{\cos \theta} r \sin \theta d r d \theta=$ ?
(a) $4 / 3$
(b) 0
(c) $\pi$
(d) $1 / 6$
10. Consider adiabatic flow of air through a duct. At a given point in the duct, velocity of air is 300 $\mathrm{m} / \mathrm{s}$, temperature is 330 K and pressure is 180 kPa . Assume that the air behaves as a perfect gas with constant $\mathrm{c}_{\mathrm{p}}=1.005 \mathrm{~kJ} / \mathrm{kg} . \mathrm{K}$. The stagnation temperature at this point is $\qquad$ K (round off to two decimal places).
11. A factory produces $m(i=1,2, \ldots, m)$ products, each of which requires processing on $n(j=1,2 \ldots$, n) workstations. Let $\mathrm{a}_{\mathrm{ij}}$ be the amount of processing time that one unit of the $\mathrm{i}^{\text {th }}$ product requires on the $j^{\text {th }}$ workstation. Let the revenue from selling one unit of the $i^{\text {th }}$ product be $r_{i}$ and $h_{i}$ be the holding cost per unit per time period for the $\mathrm{i}^{\text {th }}$ product. The planning horizon consists of $\mathrm{T}(\mathrm{t}=1,2, \ldots, \mathrm{~T})$ time periods. The minimum demand that must be satisfied in time period $t$ is $d_{i t}$, and the capacity of the $j^{\text {th }}$ workstation in time period t is $\mathrm{c}_{\mathrm{jt}}$. Consider the aggregate planning formulation below, with decision variables $S^{\text {it }}$ (amount of product i sold in time period t ), $\mathrm{X}_{\mathrm{it}}$ (amount of product $i$ manufactured in time period $t$ ) and $\mathrm{I}_{\mathrm{it}}$ (amount of product ${ }_{i}$ held in inventory at the end of time period t ).

$$
\max \sum_{t=1}^{T} \sum_{i=1}^{m}\left(r_{i} S_{i t}-h_{i} I_{i t}\right)
$$

Subject to
$\mathrm{S}_{\mathrm{it}} \geq \mathrm{d}_{\mathrm{it}} \forall \mathrm{i}, \mathrm{t}$
< capacity constraint >
< inventory balance constraint >
$X_{i t}, S_{i t}, I_{i t} \geq 0 ; I_{i 0}=0$
The capacity constraints and inventory balance constraints for this formulation respectively are
(a) $\sum_{i}^{m} a_{i j} X_{i t} \leq c_{j t} \forall j, t$ and $I_{i t}=I_{i, t-1}+X_{i t}-S_{i t} \forall i, t$
(b) $\sum_{i}^{m} a_{i j} X_{i t} \leq d_{j t} \forall i, t$ and $I_{i t}=I_{i, t-1}+X_{i t}-S_{i t} \forall i, t$
(c) $\sum_{i}^{m} a_{i j} X_{i t} \leq d_{i t} \forall i, t$ and $I_{i t}=I_{i, t-1}+X_{i t}+S_{i t}-X_{i t} \quad \forall i, t$
(d) $\sum_{i}^{m} a_{i j} X_{i t} \leq c_{j t} \forall i, t$ and $I_{i t}=I_{i, t-1}+X_{i t}-d_{i t} \forall i, t$

## TVTHE GATE COACH

12. Let the superscript T represent the transpose operation. Consider the function $f(x)=\frac{1}{2} x^{T} Q_{x}-r^{T} x$, where $x$ and r are $\mathrm{n} \times 1$ vectors and Q is a symmetric $\mathrm{n} \times \mathrm{n}$ matrix. The stationary point of $\mathrm{f}(x)$ is
(a) $\mathrm{Q}^{-1} \mathrm{r}$
(b) $Q^{T} r$
(c) r
(d) $\frac{r}{r^{T} r}$
13. A plane truss $\mathrm{PQRS}\left(\mathrm{PQ}=\mathrm{RS}\right.$, and $\angle \mathrm{PQR}=90^{\circ}$ ) is shown in the figure.


The forces in the members PR and RS, respectively, are $\qquad$
(a) $\mathrm{F} \sqrt{2}$ (tensile) and F (compressive)
(b) F (tensile) and $\mathrm{F} \sqrt{2}$ (tensile)
(c) $\mathrm{F} \sqrt{2}$ (tensile) and F (tensile)
(d) F (compressive) and $\mathrm{F} \sqrt{2}$ (compressive)
14. Value of $(1+\mathrm{i})^{8}$, where $\mathrm{i}=\sqrt{-i}$, is equal to
(a) 16
(b) 4 i
(c) 4
(d) 16 i

## TVTHE GATE COACH

15. The thickness, width and length of a metal slab are $50 \mathrm{~mm}, 250 \mathrm{~mm}$ and 3600 mm , respectively. A rolling operation on this slab reduced the thickness by $10 \%$ and increases the width by $3 \%$. The length of the rolled slab is $\qquad$ mm (round off to one decimal place).
16. The von Mises stress at a point in a body subjected to forces is proportional to the square root of the
(a) plastic strain energy per unit volume
(b) dilatational strain energy per unit volume
(c) distortional strain energy per unit volume
(d) total strain energy per unit volume.
17. The figure shows the relationship between strength ( S ) and fatigue life $(\mathrm{N})$ of a material. The fatigue strength of the material for a life of 1000 cycles is 450 MPa , while its fatigue strength for a life of $10^{6}$ cycles is 150 MPa .


The life of a cylindrical shaft made of this material subjected to an alternating stress of 200 MPa will then be $\qquad$ cycles (round off to the nearest integer).
18. Value of $\int_{4}^{5.2} \ln x d x$ using Simpson's $1 / 3^{\text {rd }}$ rule with interval size 0.3 is
(a) 1.06
(b) 1.51
(c) 1.60
(d) 1.83
19. A block of negligible mass rests on a surface that is inclined at $30^{\circ}$ to the horizontal plane as shown in the figure. When a vertical force of 900 N and a horizontal force of 750 N are applied, the block is just about to slide.


The coefficient of static friction between the block and surface is $\qquad$ (round off to two decimal places).
20. A steel cubic block of side 200 mm is subjected to hydrostatic pressure of $250 \mathrm{~N} / \mathrm{mm}^{2}$. The elastic modulus is $2 \times 10^{5} \mathrm{~N} / \mathrm{mm}^{2}$ and Poisson's ratio is 0.3 for steel. The side of the block is reduced by
$\qquad$ mm (round off to two decimal places).
21. A cantilever beam with a uniform flexural rigidity $\left(E I=200 \times 10^{6} \mathrm{~N} . \mathrm{m}^{2}\right)$ is loaded with a concentrated force at its free end. The area of the bending moment diagram corresponding to the full length of the beam is $10,000 \mathrm{~N} . \mathrm{m}^{2}$. The magnitude of the slope of the beam at its free end is
$\qquad$ micro radian (round off to the nearest integer).
22. The torque provided by an engine is given by $T(\theta)=12000+2500 \sin (2 \theta)$ N.m. where $\theta$ is the angle turned by the crank from inner dead center. The mean speed of the engine is 200 rpm and it drives a machine that provides a constant resisting torque. If variation of the speed from the mean speed is not to exceed $\pm 0.5 \%$, the minimum mass moment of inertia of the flywheel should be kg. $\mathrm{m}^{2}$ (round off to the nearest integer).
23. A rigid tank of volume $50 \mathrm{~m}^{3}$ contains a pure substance as a saturated liquid vapour mixture at 400 kPa . Of the total mass of the mixture, $20 \%$ mass is liquid and $80 \%$ mass is vapour. Properties at 400 kPa are: Saturation temperature, $\mathrm{T}_{\text {sat }}=143.61^{\circ} \mathrm{C}$; Specific volume of saturated liquid, $\mathrm{v}_{\mathrm{f}}=$ $0.001084 \mathrm{~m}^{3} / \mathrm{kg}$; Specific volume of saturated vapour, $\mathrm{vg}_{\mathrm{g}}=0.46242 \mathrm{~m}^{3} / \mathrm{kg}$. The total mass of liquid vapour mixture in the tank is $\qquad$ kg (round off to the nearest integer).

## TVTHE GATE COACH

24. For a two-dimensional, incompressible flow having velocity components $u$ and $v$ in the $x$ and $y$ directions, respectively, the expression
$\frac{\partial\left(u^{2}\right)}{\partial x}+\frac{\partial(u v)}{\partial y}$
Can be simplified to
(a) $2 u \frac{\partial u}{\partial x}+u \frac{\partial v}{\partial y}$
(b) $u \frac{\partial u}{\partial x}+u \frac{\partial v}{\partial y}$
(c) $u \frac{\partial u}{\partial x}+v \frac{\partial u}{\partial y}$
(d) $2 u \frac{\partial u}{\partial x}+v \frac{\partial u}{\partial y}$
25. Consider the system shown in the figure. A rope goes over a pulley. A mass, $m$, is hanging from the rope. A spring of stiffness, $k$, is attached at one end of the rope. Assume rope is inextensible, massless and there is no slip between pulley and rope.


The pulley radius is $r$ and its mass moment of inertia is J. Assume that the mass is vibrating harmonically about its static equilibrium position. The natural frequency of the system is
(a) $\sqrt{\frac{k r^{2}}{J+m r^{2}}}$
(b) $\sqrt{k / m}$
(c) $\sqrt{\frac{k r^{2}}{J}}$
(d) $\sqrt{\frac{k r^{2}}{J-m r^{2}}}$
26. A shell and tube heat exchanger is used as a steam condenser. Coolant water enters the tube at 300 K at a rate of $100 \mathrm{~kg} / \mathrm{s}$. The overall heat transfer coefficient is $1500 \mathrm{~W} / \mathrm{m}^{2} . \mathrm{K}$, and total heat transfer area is $400 \mathrm{~m}^{2}$. Steam condenses at a saturation temperature of 350 K . Assume that the specific heat of coolant water is $4000 \mathrm{~J} / \mathrm{kg} . \mathrm{K}$. The temperature of the coolant water coming out of the condenser is
$\qquad$ K (round off to the nearest integer).
27. A machine of mass 100 kg is subjected to an external harmonic force with a frequency of $40 \mathrm{rad} / \mathrm{s}$. The designer decides to mount the machine on an isolator to reduce the force transmitted to the foundation. The isolator can be considered as a combination of stiffness ( K ) and damper (damping factor, $\xi$ ) in parallel. The designer has the following four isolators:
(1) $\mathrm{K}=640 \mathrm{kN} / \mathrm{m}, \xi=0.70$
(2) $\mathrm{K}=640 \mathrm{kN} / \mathrm{m}, \xi=0.07$
(3) $\mathrm{K}=22.5 \mathrm{kN} / \mathrm{m}, \xi=0.70$
(4) $\mathrm{K}=22.5 \mathrm{kN} / \mathrm{m}, \xi=0.07$

Arrange the isolators in the ascending order of the force transmitted to the foundation.
(a) 1-3-4-2
(b) 1-3-2-4
(c) 4-3-1-2
(d) 3-1-2-4
28. A column with one end fixed and one end free has a critical buckling load of 100 N . For the same column, if the free end is replaced with a pinned end then the critical buckling load will be $\qquad$ N (round off to the nearest integer).
29. A spot welding operation performed on two pieces of steel yielded a nugget with a diameter of 5 mm and a thickness of 1 mm . The welding time was 0.1 s . The melting energy for the steel is 20 $\mathrm{J} / \mathrm{mm}^{3}$. Assuming the heat conversion efficiency as $10 \%$, the power required for performing the spot welding operation is $\qquad$ kW (round off to two decimal places).
30. The mean and variance, respectively, of a binomial distribution for n independent trials with the probability of success as $p$, are

## TVTHE GATE COACH

(a) np, np
(b) $\mathrm{np}, \mathrm{np}(1-\mathrm{p})$
(c) $\sqrt{n p}, \mathrm{np}(1-2 \mathrm{p})$
(d) $\sqrt{n p}, \sqrt{n p(1-p)}$
31. The wheels and axle system lying on a rough surface is shown in the figure.


Each wheel has diameter 0.8 m and mass 1 kg . Assume that the mass of the wheel is concentrated at rim and neglect the mass of the spokes. The diameter of axle is 0.2 m and its mass is 1.5 kg . Neglect the moment of inertia of the axle and assume $\mathrm{g}=9.8 \mathrm{~m} / \mathrm{s}^{2}$. An effort of 10 N is applied on the axle in the horizontal direction shown at mid span of the axle. Assume that the wheels move on a horizontal surface without slip. The acceleration of the wheel axle system in horizontal direction is
$\qquad$ $\mathrm{m} / \mathrm{s}^{2}$ (round off to one decimal place).
32. A high velocity water jet of cross sectional area $=0.01 \mathrm{~m}^{2}$ and velocity $=35 \mathrm{~m} / \mathrm{s}$ enters a pipe filled with stagnant water. The diameter of the pipe is 0.32 m . This high velocity water jet entrains additional water from the pipe and the total water leaves the pipe with a velocity $6 \mathrm{~m} / \mathrm{s}$ as shown in the figure.

The flow rate of entrained water is $\qquad$ litres/s (round off to two decimal places).

THE GATE COACH


The flow rate of entrained water is $\qquad$ litres/s (round off to two decimal places).
33. Consider an $\mathrm{n} \times \mathrm{n}$ matrix A and a non-zero $\mathrm{n} \times 1$ vector p . Their product $\mathrm{Ap}=\alpha^{2} \mathrm{p}$, where $\alpha \in \Re$ and $\alpha \notin\{-1,0,1\}$. Based on the given information, the Eigen value of $A^{2}$ is :
(a) $\alpha^{4}$
(b) $\alpha$
(c) $\sqrt{\alpha}$
(d) $\alpha^{2}$
34. The demand and forecast of an item for five months are given in the table.

| Month | Demand | Forecast |
| :---: | :---: | :---: |
| April | 225 | 200 |
| May | 220 | 240 |
| June | 285 | 300 |
| July | 290 | 270 |
| August | 250 | 230 |

The Mean absolute Percent Error (MAPE) in the forecast is $\qquad$ \% (round off to two decimal places).
35. Water flows out from a large tank of cross-sectional area $A_{t}=1 \mathrm{~m}^{2}$ through a small rounded orifice of cross-sectional area $A_{0}=1 \mathrm{~cm}^{2}$, located at $y=0$. Initially the water level $(H)$, measured from $\mathrm{y}=0$, is 1 m . The acceleration due to gravity is $9.8 \mathrm{~m} / \mathrm{s}^{2}$.


Neglecting any loses, the time taken by water in the tank to reach a level of $y=H / 4$ is $\qquad$ seconds (round off to one decimal place).
36. Ambient air flows over a heated slab having flat, top surface at $y=0$. The local temperature (in Kelvin) profile within the thermal boundary layer is given by $\mathrm{T}(\mathrm{y})=300+200 \exp (-5 \mathrm{y})$, where y is the distance measured from the slab surface in metres. If the thermal conductivity of air is $1.0 \mathrm{~W} / \mathrm{m} . \mathrm{K}$ and that of the slab is $100 \mathrm{~W} / \mathrm{m} . \mathrm{K}$, then the magnitude of temperature gradient $|\mathrm{dT} / \mathrm{dy}|$ within the slab at $\mathrm{y}=0$ is $\qquad$ $\mathrm{K} / \mathrm{m}$ (round off to the nearest integer).
37. A PERT network has 9 activities on its critical path. The standard deviation of each activity on the critical path is 3 . The standard deviation of the critical path is
(a) 9
(b) 81
(c) 27
(d) 3
38. Which of the following is responsible for eddy viscosity (or turbulent viscosity) in a turbulent boundary layer on a flat plate?
(a) Reynolds stresses
(b) Boussinesq stresses
(c) Nikuradse stresses
(d) Prandtl stresses
39. In a pure orthogonal turning by a zero rake angle single point carbide cutting tool, the shear force has been computed to be 400 N . If the cutting velocity, $\mathrm{V}_{\mathrm{c}}=100 \mathrm{~m} / \mathrm{min}$, depth of cut, $\mathrm{t}=2.0 \mathrm{~mm}$,
feed, $\mathrm{s}_{\mathrm{o}}=0.1 \mathrm{~mm} /$ revolution and chip velocity, $\mathrm{V}_{\mathrm{f}}=20 \mathrm{~m} / \mathrm{min}$, then the shear strength, $\tau_{\mathrm{s}}$ of the material will be $\qquad$ MPa (round off to two decimal places).
40. Daily production capacity of a bearing manufacturing company is 30,000 bearings. The daily demand of the bearing is 15,000 . The holding cost per year of keeping a bearing in the inventory is Rs. 20. The setup cost for the production of a batch is Rs. 1800. Assuming 300 working days in a year, the economic batch quantity in number of bearing is $\qquad$ (in integer).
41. Consider the open feed water heater (FWH) shown in the figure given below:


Specific enthalpy of steam at location 2 is $\mathrm{kJ} / \mathrm{kg}$, specific enthalpy of water at location 5 is 226.7 $\mathrm{kJ} / \mathrm{kg}$. If the mass flow rate of water entering the open feed water heater (at location 5) is $100 \mathrm{~kg} / \mathrm{s}$ then the mass flow rate of steam at location 2 will be $\qquad$ $\mathrm{kg} / \mathrm{s}$ (round off to one decimal place).
42. A surface grinding operation has been performed on a Cast Iron plate having dimensions 300 mm (length) $\times 10 \mathrm{~mm}$ (width) $\times 50 \mathrm{~mm}$ (height). The grinding was performed using an alumina wheel having a wheel diameter of 150 mm and wheel width of 12 mm . The grinding velocity used is $40 \mathrm{~m} / \mathrm{s}$, table speed is $5 \mathrm{~m} / \mathrm{min}$, depth of cut per pass is $50 \mu \mathrm{~m}$ and the number of grinding passes is 20 . The average tangential and average normal forces for each pas are found to be 40 N and 60 N respectively. The value of the specific grinding energy under the aforesaid grinding conditions is $\qquad$ $\mathrm{J} / \mathrm{mm}^{3}$ (round off to one decimal place).
43. A plane frame PQR (fixed at P and free at R ) is shown in the figure. Both members ( PQ and QR ) have length, L, and flexural rigidity, EI. Neglecting the effect of axial stress and transverse shear, the horizontal deflection at free end, R , is

(a) $\frac{5 \mathrm{FL}^{3}}{3 \mathrm{EI}}$
(b) $\frac{\mathrm{FL}^{3}}{3 \mathrm{EI}}$
(c) $\frac{2 \mathrm{FL}^{3}}{3 \mathrm{EI}}$
(d) $\frac{4 \mathrm{FL}^{3}}{3 \mathrm{EI}}$
44. The size distribution of the powder particles used in Powder Metallurgy process can be determined by
(a) Laser reflection
(b) Laser penetration
(c) Laser absorption
(d) Laser scattering
45. The machining process that involves ablation is
(a) Electrochemical Machining
(b) Abrasive Jet Machining
(c) Chemical Machining
(d) Laser Beam Machining
46. If the Laplace Transform of a function $\mathrm{f}(\mathrm{t})$ is given by $\frac{s+3}{(s+1)(s+2)}$, then $\mathrm{f}(0)$ is
(A) $3 / 2$
(B) $1 / 2$
(C) 0
(D) 1
47. A vertical shaft Francis turbine rotates at 300 rpm . The available head at the inlet to the turbine is 200 m . The tip speed of the rotor is $40 \mathrm{~m} / \mathrm{s}$. Water leaves the runner of the turbine without whirl. Velocity at the exit of the draft tube is $3.5 \mathrm{~m} / \mathrm{s}$. The head losses in different components of the turbine are: (i) stator and guide vanes: 5.0 m , (ii) rotor: 10 m , and (iii) draft tube: 2 m . Flow rate through the turbine is $20 \mathrm{~m}^{3} / \mathrm{s}$. Take $g=9.8 \mathrm{~m} / \mathrm{s}^{2}$. The hydraulic efficiency of the turbine is $\qquad$ \% (round off to one decimal place).
48. Ambient pressure, temperature and relative humidity at a location are $101 \mathrm{kPa}, 300 \mathrm{~K}$, and $60 \%$, respectively. The saturation pressure of water at 300 K is 3.6 kPa . The specific humidity of ambient air is $\qquad$ $\mathrm{g} / \mathrm{kg}$ of dry air.
(a) 35.1
(b) 21.4
(c) 13.6
(d) 21.9
49. In forced convective heat transfer, Stanton number ( St ), Nusselt number ( Nu ), Reynolds number $(\mathrm{Re})$ and Prandtl number ( Pr ) are related as
(a) $\mathrm{St}=\mathrm{Nu} \operatorname{Pr} \mathrm{Re}$
(b) $\mathrm{St}=\frac{\mathrm{Nu} \mathrm{Pr}}{\mathrm{Re}}$
(c) $\mathrm{St}=\frac{\mathrm{NuRe}}{\mathrm{Pr}}$
(d) $\mathrm{St}=\frac{\mathrm{Nu}}{\mathrm{RePr}}$
50. Consider the following differential equation,
$(1+y) \frac{d y}{d x}=y$

The solution of the equation that satisfies the condition $y(1)=1$ is
(a) $y^{2} \mathrm{e}^{y}=\mathrm{e}^{x}$

## TVTHE GATE COACH

(b) $\mathrm{ye}^{y}=\mathrm{e}^{x}$
(c) $2 y^{y}=e^{x}+e$
(d) $(1+y) \mathrm{e}^{y}=2 \mathrm{e}^{x}$
51. An object is moving with a Mach number of 0.6 in an ideal gas environment, which is at a temperature of 350 K . The gas constant is $320 \mathrm{~J} / \mathrm{kg} . \mathrm{K}$ and ratio of specific heats is 1.3 . The speed of object is $\qquad$ $\mathrm{m} / \mathrm{s}$ (round off to the nearest integer).
52. A two dimensional flow has velocities in $x$ and $y$ directions given by $u=2 x y t$ and $v=-y^{2} t$, where t denotes time. The equation for streamline passing through $x=1, y=1$ is
(a) $x^{2} y^{2}=1$
(b) $x y^{2}=1$
(c) $x^{2} y=1$
(d) $x / y^{2}=1$
53. Consider the mechanism shown in the figure. There is rolling contact without slip between the disc and ground.


Select the correct statement about instantaneous centers in the mechanism.
(a) All points $P, Q, R, S, T$ and $U$ are instantaneous centers of mechanism
(b) Only points $\mathrm{P}, \mathrm{Q}$ and S are instantaneous centers of mechanism
(c) Only points $\mathrm{P}, \mathrm{Q}, \mathrm{S}$ and T are instantaneous centers of mechanism
(d) Only points $\mathrm{P}, \mathrm{Q}, \mathrm{R}, \mathrm{S}$ and U are instantaneous centers of mechanism
54. The controlling force curves $\mathrm{P}, \mathrm{Q}$ and R for a spring controlled governor are shown in the figure, where $r_{1}$ and $r_{2}$ are any two radii of rotation.


The characteristic shown by the curves are
(a) P - Unstable; Q - Isochronous; R - Stable
(b) P - Unstable; Q - Stable; R - Isochronous
(c) P - Stable; Q - Isochronous; R - Unstable
(d) P - Stable; Q - Unstable; R- Isochronous
55. A 76.2 mm gauge block is used one end of a 254 mm sine bar with roll diameter of 25.4 mm . The height of gauge blocks required at the other end of the sine bar to measure an angle of $30^{\circ}$ is
$\qquad$ mm (round off to two decimal places).

